

Solving Systems - By Substitution

Solve the following systems of equations by substitution:

$$\begin{aligned}
 1. \quad & y = x + 10 \\
 & 4x + 5y = -13 \\
 & 4x + 5(x + 10) = -13 \\
 & 4x + 5x + 50 = -13 \\
 & 9x + 50 = -13 \\
 & \quad \underline{-50} \quad \underline{-50} \\
 & \quad \cancel{9}x = \frac{-63}{\cancel{9}} \\
 & \quad \boxed{x = -7} \\
 & y = (-7) + 10 \\
 & \quad \boxed{y = 3} \\
 & \boxed{(-7, 3)}
 \end{aligned}$$

$$\begin{aligned}
 2. \quad & c = 1 - d \\
 & 3d - 2c = -17 \\
 & 3d - 2(1 - d) = -17 \\
 & 3d - 2 + 2d = -17 \\
 & 5d - 2 = -17 \\
 & \quad \underline{+2} \quad \underline{+2} \\
 & \quad \cancel{5}d = \frac{-15}{\cancel{5}} \\
 & \quad \boxed{d = -3} \\
 & c = 1 - (-3) \\
 & \quad \boxed{c = 4} \\
 & \boxed{(4, -3)}
 \end{aligned}$$

$$\begin{aligned}
 3. \quad & m - n = -10 \\
 & n = 3m + 20 \\
 & m - (3m + 20) = -10 \\
 & m - 3m - 20 = -10 \\
 & -2m - 20 = -10 \\
 & \quad \underline{+20} \quad \underline{+20} \\
 & \quad \cancel{-2}m = \frac{10}{\cancel{-2}} \\
 & \quad \boxed{m = -5} \\
 & n = 3(-5) + 20 \\
 & n = -15 + 20 \\
 & \quad \boxed{n = 5} \\
 & \boxed{(-5, 5)}
 \end{aligned}$$

$$\begin{aligned}
 4. \quad & x - 2y = 0 \\
 & 5x + 6y = 16 \\
 & x - 2y = 0 \\
 & \quad \underline{+2y} \quad \underline{+2y} \\
 & \quad x = 2y \\
 & 5(2y) + 6y = 16 \\
 & 10y + 6y = 16 \\
 & \quad \underline{16y} = \frac{16}{\cancel{16}} \\
 & \quad \boxed{y = 1} \\
 & x = 2(1) \\
 & \quad \boxed{x = 2} \\
 & \boxed{(2, 1)}
 \end{aligned}$$

$$\begin{aligned}
5. \quad & a + b = -7 \\
& 5a - 2b = 7 \\
& a + b = -7 \\
& \quad \underline{-b} \quad \underline{-b} \\
& a = -b - 7 \\
& 5(-b - 7) - 2b = 7 \\
& -5b - 35 - 2b = 7 \\
& -7b - 35 = 7 \\
& \quad \underline{+35} \quad \underline{+35} \\
& \quad \cancel{-7b} = \frac{42}{\cancel{-7}} \\
& \quad \boxed{b = -6} \\
& a = -(-6) - 7 \\
& a = 6 - 7 \\
& \quad \boxed{a = -1} \\
& \boxed{(-1, -6)}
\end{aligned}$$

$$\begin{aligned}
6. \quad & 5p - 3q = 9 \\
& 8p + q = -3 \\
& \quad \underline{-8p} \quad \underline{-8p} \\
& \quad \quad q = -8p - 3 \\
& 5p - 3(-8p - 3) = 9 \\
& 5p + 24p + 9 = 9 \\
& 29p + 9 = 9 \\
& \quad \underline{-9} \quad \underline{-9} \\
& \quad \frac{29p}{\cancel{29}} = \frac{0}{\cancel{29}} \\
& \quad \quad \boxed{p = 0} \\
& q = -8(0) - 3 \\
& q = 0 - 3 \\
& \quad \boxed{q = -3} \\
& \boxed{(0, -3)}
\end{aligned}$$

$$\begin{aligned}
7. \quad & 2x = y - 1 \\
& 2y = 1 + 4x \\
& 2x = y - 1 \\
& \quad \underline{+1} \quad \underline{+1} \\
& 2x + 1 = y \\
& 2(2x + 1) = 1 + 4x \\
& 4x + 2 = 1 + 4x \\
& \quad \underline{-4x} \quad \quad \underline{-4x} \\
& 2 = 1 \\
& \quad \boxed{\emptyset}
\end{aligned}$$

$$\begin{aligned}
8. \quad & -j + 3k = 14 \\
& 2j - 9k = -40 \\
& -j + 3k = 14 \\
& \quad \underline{-3k} \quad \underline{-3k} \\
& \quad \frac{\cancel{-j}}{\cancel{-1}} = \frac{-3k + 14}{-1} \\
& \quad \quad j = 3k - 14 \\
& 2(3k - 14) - 9k = -40 \\
& 6k - 28 - 9k = -40 \\
& -3k - 28 = -40 \\
& \quad \underline{+28} \quad \underline{+28} \\
& \quad \frac{\cancel{-3k}}{\cancel{-3}} = \frac{-12}{-3} \\
& \quad \quad \boxed{k = 4} \\
& j = 3(4) - 14 \\
& j = 12 - 14 \\
& \quad \boxed{j = -2} \\
& \boxed{(-2, 4)}
\end{aligned}$$

$$9. \quad 7g - 5h = 1$$

$$5 - h = -4g$$

$$\begin{array}{r} -5 \quad -5 \\ \hline \cancel{h} = \frac{-4g - 5}{-1} \end{array}$$

$$h = 4g + 5$$

$$7g - 5(4g + 5) = 1$$

$$7g - 20g - 25 = 1$$

$$-13g - 25 = 1$$

$$\begin{array}{r} +25 \quad +25 \\ \hline \cancel{-13g} = \frac{26}{\cancel{-13}} \end{array}$$

$$\boxed{g = -2}$$

$$h = 4(-2) + 5$$

$$h = -8 + 5$$

$$\boxed{h = -3}$$

$$\boxed{(-2, -3)}$$

$$10. \quad 6x - y = 2$$

$$2y + 4 = 12x$$

$$6x - y = 2$$

$$\begin{array}{r} -6x \quad -6x \\ \hline \cancel{y} = \frac{-6x + 2}{-1} \end{array}$$

$$y = 6x - 2$$

$$2(6x - 2) + 4 = 12x$$

$$12x - 4 + 4 = 12x$$

$$\begin{array}{r} \cancel{12x} = \frac{\cancel{12x}}{\cancel{12}} \end{array}$$

$$x = x$$

$$\boxed{\{(x, y) : 6x - y = 2\}}$$